



An Experimental Kalman Filter Approach to the International Terrestrial Reference Frame Realization

***X. “Frank” Wu¹, Claudio Abbondanza¹, Zuheir Altamimi²,
T. Mike Chin¹, Richard Gross¹, and Mike Heflin¹***

1. Jet Propulsion Laboratory, California Institute of Technology, USA
2. Institut National de l'Information Geographique et Forestiere, France

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Current ITRF Status and Rationale

- **Secular frame characterized by X , V and a full covariance matrix**
 - Linear motion models for all sites
 - Origin at mean but not instantaneous CM
 - CM for secular motion
 - Close to CF for sub-secular motions
 - The linear motion model works very well and the ITRF2008 frame is quite stable at 0.3 – 0.5 mm/yr
- **The case for an Experimental Kalman Filter Approach**
 - Non-linear motion, sites with short data span
 - Near real-time orbit determination and global monitoring
 - Unify different geodetic data time series in one and the same frame
 - Origin at nearly instantaneous CM



Experimental Kalman Filter Approach to TRF

- **One reference frame** realized by time series
- **Origin defined at weekly (nearly instantaneous) CM**
 - Currently through SLR data
 - Could take other data or models in the future
- **Scale realized by weekly SLR/VLBI data**
- **Orientation defined weekly by convention and no net rotation**
- **Local ties are applied only once in the weeks of surveying or within the continuous segments without offsets**
- **Co-motion constraints are applied to most if not all co-located sites**



Weekly Combination Strategy

- Use CATREF heritage
- Combination done at weekly basis
- Kalman Filter Data Update

- Coordinates in file k

$$X_s^i = X_c^i + (t_s^i - t_0) \dot{X}_c^i + T_k + D_k X_c^i + R_k X_c^i \\ + (t_s^i - t_k) [\dot{T}_k + \dot{D}_k X_c^i + \dot{R}_k X_c^i]$$

- Local Ties applied once

- Tight Orientation Constraints every week

$$0 = B(X_c - X_r)$$

- Weekly displacements at most co-located sites are constrained to be the same

EOP in file k

$$x_s^p = x_c^p + R2_k \\ y_s^p = y_c^p + R1_k \\ UT_s = UT_c - \frac{1}{f} R3_k \\ \dot{x}_s^p = \dot{x}_c^p \\ \dot{y}_s^p = \dot{y}_c^p \\ LOD_s = LOD_c$$



Time Update or Prediction

- **Coordinate Decomposition**

$$\mathbf{X}_c = \begin{pmatrix} X_c^1 \\ Y_c^1 \\ Z_c^1 \\ \vdots \\ X_c^i \\ \vdots \end{pmatrix} = \mathbf{X} + \mathbf{S}_p$$

- **Equation of Dynamics**
- **Time Update or State Transition**

$$\begin{bmatrix} X_k \\ V_k \\ S_k^{next} \\ S_k^{now} \end{bmatrix} = \begin{bmatrix} 1 & dt & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 2e^{-dt/\tau} \cos 2\pi \frac{dt}{T} & -e^{-2dt/\tau} \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} X_{k-1} \\ V_{k-1} \\ S_{k-1}^{next} \\ S_{k-1}^{now} \end{bmatrix} + \begin{bmatrix} \varepsilon_x \\ \varepsilon_v \\ \varepsilon_p \\ 0 \end{bmatrix}$$

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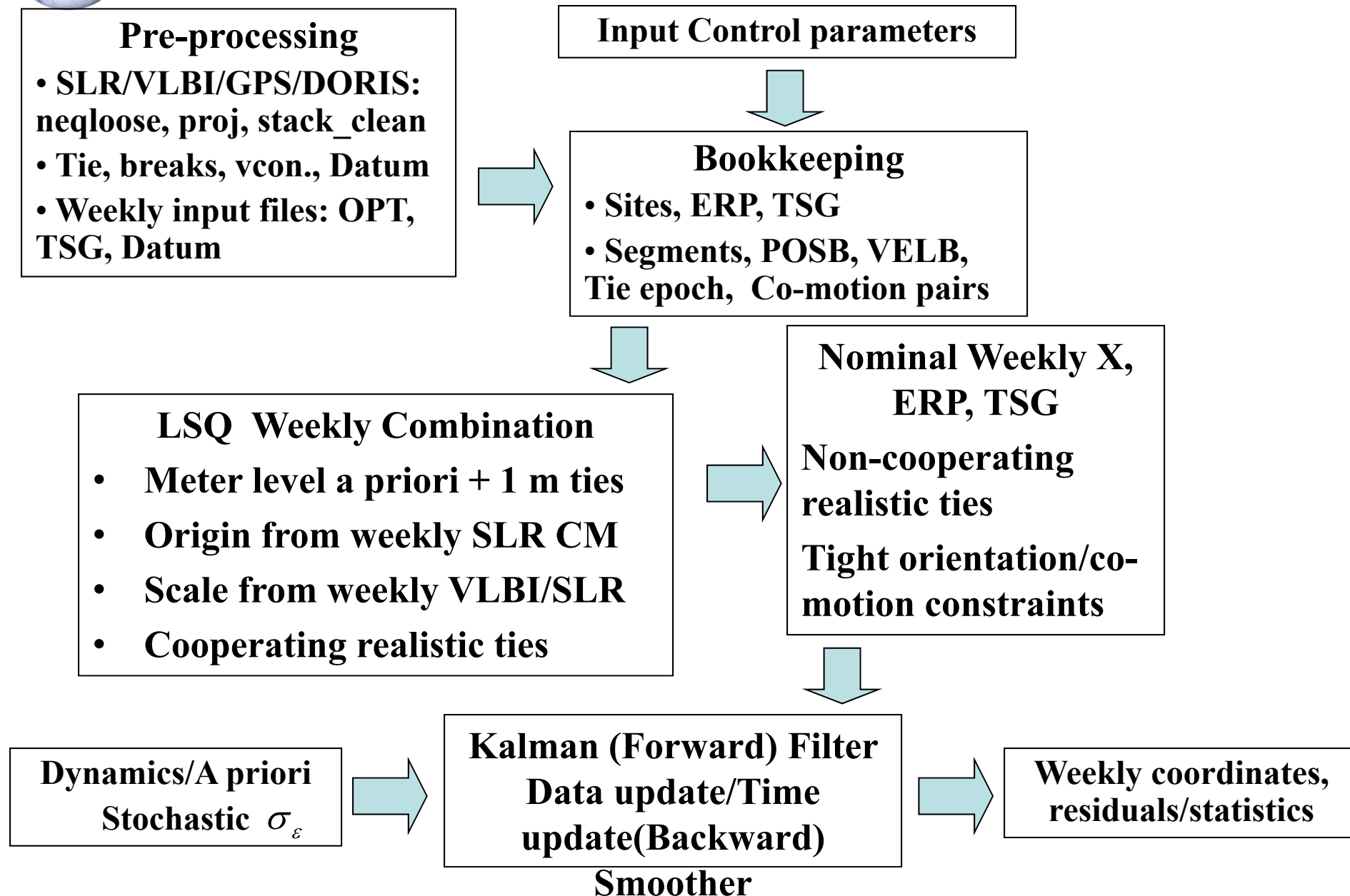
Abbondanza et al.

$$\mathbf{EOP}_k = \mathbf{EOP}_{k-1} + \varepsilon_{\mathbf{EOP}}$$

$$\mathbf{T}_k = \mathbf{T}_{k-1} + \varepsilon_{\mathbf{T}}$$

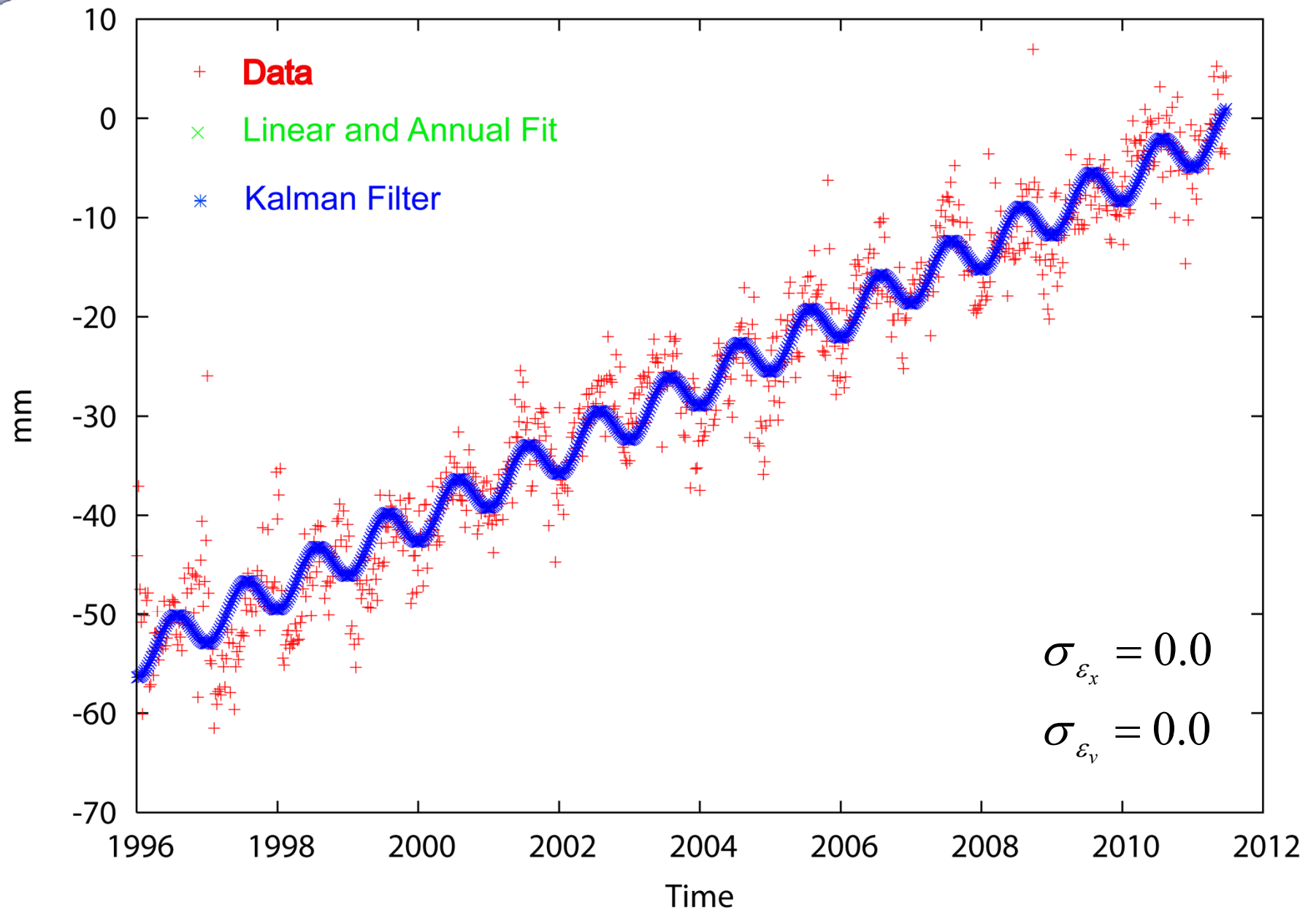


Flow Chart of Weekly Combination Filter-Smoother



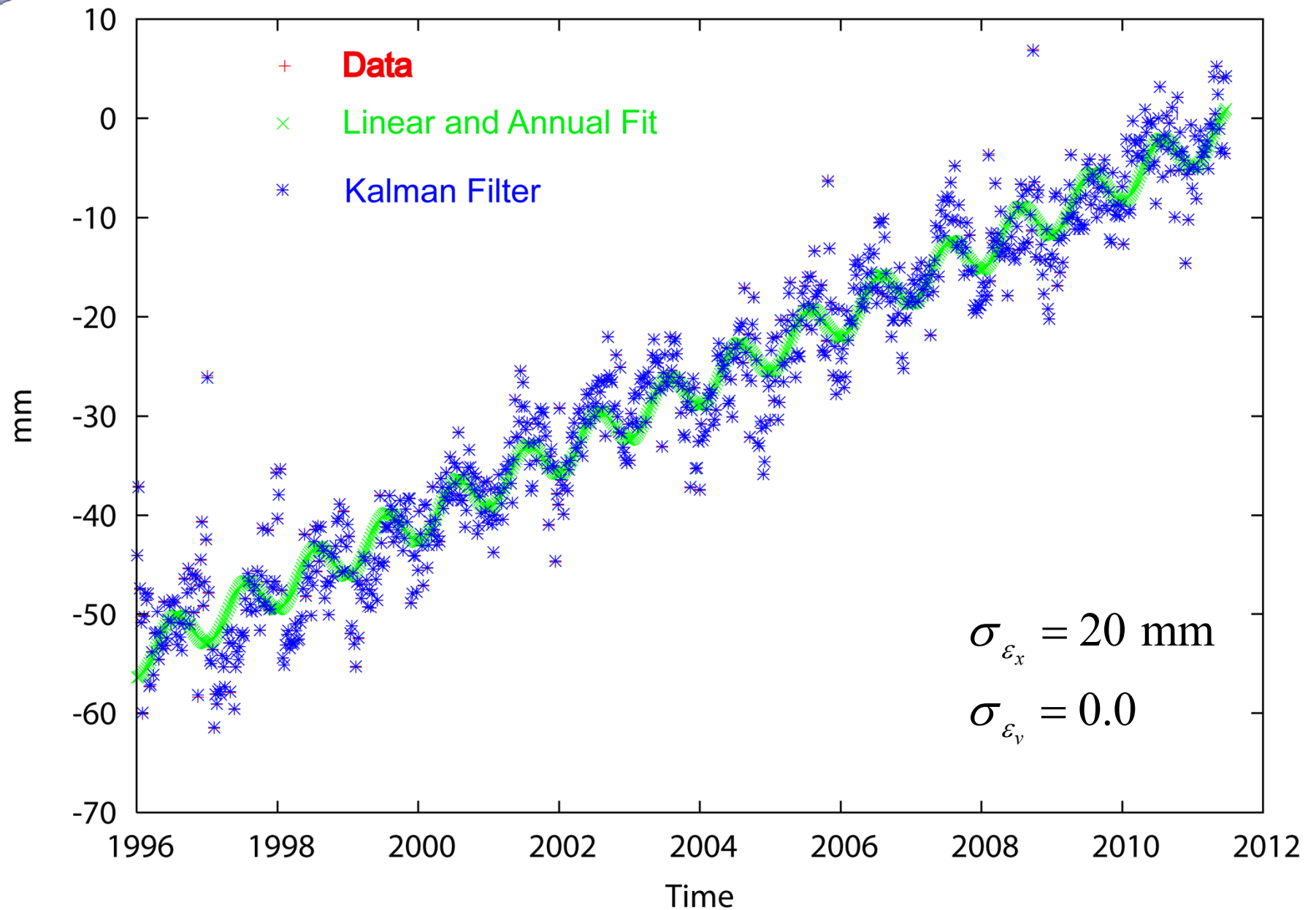


Kalman Filter and RTS Smoother



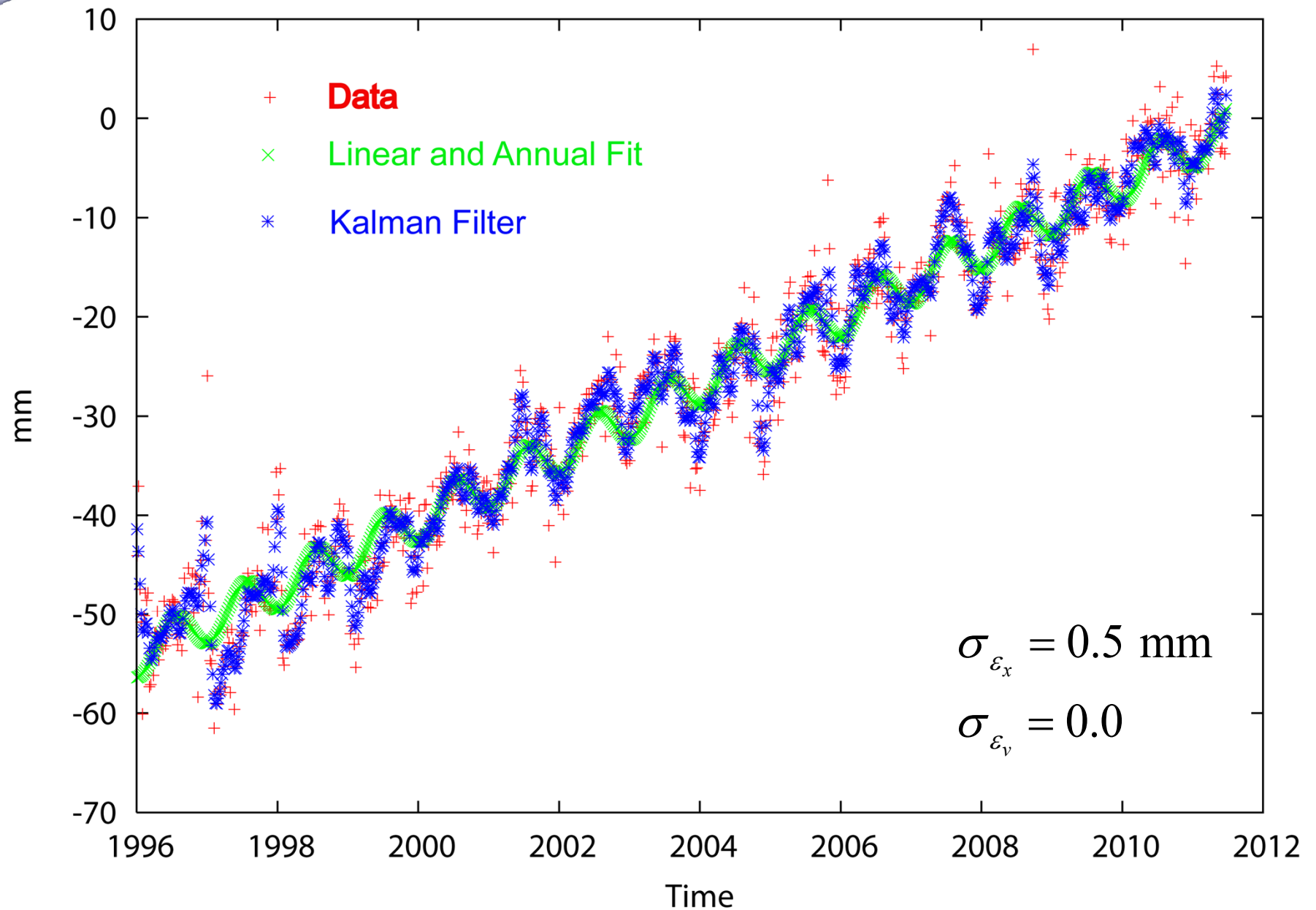


Kalman Filter and RTS Smoother





Kalman Filter and RTS Smoother





Transformation Parameters between ITRF2005 and Weekly Combination (1996-2005)

No Annual Components

Tx (mm)	Ty (mm)	Tz (mm)	D (ppb)	Rx (μ as)	Ry (μ as)	Rz (μ as)
0.1	-0.1	-0.4	-0.69	-26	-1	11
Vx (mm/y)	Vy (mm/y)	Vz (mm/y)	(ppb/y)	\dot{R}_x (μ as/y)	\dot{R}_y (μ as/y)	\dot{R}_z (μ as/y)
0.0	0.0	0.3	0.00	10	-5	3

With Annual Components

Tx (mm)	Ty (mm)	Tz (mm)	D (ppb)	Rx (μ as)	Ry (μ as)	Rz (μ as)
0.1	0.1	-0.4	-0.65	-26	-2	11
Vx (mm/y)	Vy (mm/y)	Vz (mm/y)	(ppb/y)	\dot{R}_x (μ as/y)	\dot{R}_y (μ as/y)	\dot{R}_z (μ as/y)
0.0	0.0	0.2	-0.01	10	-5	3



Summary

- Consistently and accurately defined and realized TRF is essential for global change monitoring
- Experimental TRF realized by nearly instantaneous geocentric time series and combinations are done weekly
- The Kalman filter and RTS smoother offer great power and flexibility to estimate time-dependent parameters. Easy on constraints over variables such as displacements
- Fragmented time series at co-located sites are unified dynamically
- Time series from different geodetic techniques are unified in the same frame